



Calculation Policy:

Maths at St. Mary's

St. Mary's curriculum follows the Mastery approach and we aim to...

- Teach less, learn more: less teacher talk and more evidencing work and progress.
- Ensure that no child is left behind: all children are enabled to keep up every day.
- Provide space and time to experience and apply, with all children entitled to additional support to ensure they do not fall behind or to go deeper.
- Use real life applications wherever possible to make learning relevant and not abstract; nothing should be taught without a purpose.
- Teach all children in class, together, most of the time.
- Organise children working in mixed ability pairs/groups.
- Give verbal feedback during lessons and intervention sessions, shortened comments in books and more ticking of correct concepts.
- Spend longer on one idea.
- Give children who need it additional support during same day intervention sessions.

Early Years Maths

In Nursery and Reception, we use Number Sense to deliver the number teaching of the Statutory Framework alongside the Numberblocks and NCETM resources.

Our <u>non-number</u> teaching is carefully mapped out across the year using the following resources as guidance to support planning the provision.

Spatial reasoning (covering shape and space): Early Childhood Maths Group materials https://earlymaths.org/spatial-reasoning/

Pattern: https://www.ncetm.org.uk/classroom-resources/ey-pattern/ Measures: https://www.ncetm.org.uk/classroom-resources/ey-pattern/

In Nursery and Reception the children have daily maths inputs lasting about 15 minutes that have a strong focus on talk and reasoning and encouraging children to look for patterns. Beyond this session, the teacher carefully plans continuous provision and provocation activities that support the number and non-number focuses.

The teacher will plan for one or two sessions of teacher led activities, where each child will take part and engage in practical, talk based activities that occasionally will lead to written outcomes but shall be carefully monitored by the teacher as to whether any child requires further targeted support.

Alongside the daily maths sessions, there will be daily mathematical routines that help the children develop their maths understanding. Some examples of these daily routines are; Counting songs, register on a /daily tens frame, Numberblocks episodes, daily 'name the day/month' calendar activities etc





Key Stage I Maths

In Year I & Year 2 we follow the NCETM Prioritisation Curriculum. This resource covers the National Curriculum (apart from 'Roman numerals' and 'Constructing and presenting data' which has been addressed and added to the school's long term plans) however lends a focus to the 'priority areas' known as the Ready-to- Progress Criteria from the DfE guidance.

Each Unit is crafted by the teachers using the NCETM PowerPoints as a starting point and additional resources such as Third Space Learning. Low threshold, high ceiling activities are designed across each year group and at different points to allow the children to delve deeper into each area and encourage the use of mathematical thinking and vocabulary.

To build fact fluency in KSI, Number sense is delivered daily for 15 minutes which focuses on a systematic and structured approach to develop children's understanding of number and number relationships in addition and subtraction. Below you will find the Calculation Strategies the children will be taught within the programme and encouraged to use throughout their years at St. Mary's. (page 3)

In addition to Number Sense, daily Mathematical routines such as; Third Space 'Fluent in Five' Activities, Tens Frame Registers etc are visited to highlight the ubiquity of Mathematics.

Key Stage 2

As with Key Stage 1, Key Stage 2 also follow the NCETM Prioritisation Curriculum focusing on the 'Priority areas' and is carefully mapped out to ensure progression. In addition to this, Year 3 & 4 teach Roman Numerals as a separate unit (using Third Space Resources) and within History lessons. Constructing and Presenting Data is delivered through Third Space learning with consideration to any skills needed in Science Units; where the teacher will ensure the children are taught the necessary skills before the science lesson so the application of these skills doesn't hinder the science focus. In Year 3 & Year 4, the Number Sense Times Tables Programme is followed. This is a highly visual approach to learning the essential Multiplication and Division facts and concepts. It focuses on teaching the 36 essential facts and then using them to know the commutative multiplication facts and the inverse division facts. For children moving into Year 5 & 6 who need additional time to learn the times tables facts, the teachers use the Number sense Intervention Programme either as a class or individually to address any gaps.

An example of the 36 facts can be seen below on page 4.

Daily Mathematical routines in Key Stage 2 include; Third Space 'Fluent in Five', Third Space Daily Maths Challenge and Review/Retrieve activities focusing on the 4 Operations.





Calculation Strategies

One More, One Less	When we add one, we get the next counting number.	Number Neighbours	Adjacent numbers have a difference of 1. Adjacent
*1	When we subtract one, we get the previous counting	Spot the Difference	odds and evens have a difference of 2.
	number (e.g. $5 - 1 = 4$).	4 3	Spot number neighbours (adjacent, odds or evens) to
1 2 3 4 5 6			solve subtractions of adjacent numbers (e.g. $5 - 4 = 1$),
			of adjacent odds (e.g. 9 - 7 = 2) or adjacent evens (e.g.
-1		<u> </u>	6 – 4 = 2)
Two More, Two Less:	If we add two to a number, we go from odd to next odd	7 Tree and 9 Square	Use these visual images to remember addition and
Think Odds and Evens	or even to next even. If we subtract two from a	•	subtractions fact families that children can find tricky.
+2	number, we go from odd to previous odd or even to	00 •00	For example, visualising the 7 tree helps remember that
	previous even.	• • • • • • • • • • • • • • • • • • • •	7 - 3 = 4. Visualising the 9 square helps remember that
1 3 5 7		• •00	3 + 6 = 9.
~_2		•	
Number 10 Fact	Go beyond just recalling the pairs of numbers that add	Ten and A Bit	The numbers 11 – 20 are made up of 'Ten and a Bit'.
Families	to 10. Make sure that we can also spot additions and		Recognising and understanding the 'Ten and a Bit'
(10)	subtractions which we can use number bonds to 10 to		structure of these numbers enables addition and
	solve.		subtraction facts involving their constituent parts (e.g. 3
2 2			+ 10 = 13, 17 - 7 = 10, 12 - 10 = 2).
Five and A Bit	The numbers 6, 7, 8 and 9 are made up of five and a	Make Ten and Then	Additions which cross the 10 boundary can be
Five and H Bit	bit'. This can be shown on hands, and supports	Make ren and rnen	calculated by 'Making Ten' first, and then adding on the
	decomposition of these numbers into their five and a bit		remaining amount (e.g. 8 + 6 can be calculated by
1 6.00	parts (e.g. $5 + 3 = 8$, $9 - 5 = 4$).		thinking '8 + 2 = 10 and 4 more makes 14'). The same
	parts (c.g. 5 × 5 × 5, 5 × 7).		strategy can be applied to subtractions through 10.
			37
Know about 0	When we add 0 to or subtract 0 from another number,	Adjust It	Any addition and subtraction can be calculated by
	the total remains the same. If we subtract a number	+10	adjusting from a fact you know already, (e.g. 6 + 9 is one
	from itself, the difference is 0.	10	less than 6 + 10).
		-1	
Doubles and	Memorise doubles of numbers to 10, using a visual	Swap It	When the order of two numbers being added (addends)
Near Doubles	approach. Then use these known double facts to		is exchanged the total remains the same. E.g. $1 + 8 = 8$
	calculate near doubles and hidden doubles. Once we	// \\	+ 1. Sometimes reversing the order of the two addends
	know $6 + 6 = 12$ then $6 + 7$ and $5 + 7$ is easy.	1	makes addition easier to think about conceptually.
		1 + 6	



3 times

4 times

5 times

6 times

7 times

8 times

2 times

St. Mary's Catholic Primary School

9 times



| tables |
|------------|------------|------------|------------|------------|------------|------------|------------|
| | | | | | | | |
| | | | | | | | |
| 2 x 2 = 4 | | | | | | | |
| 3 x 2 = 6 | 3 x 3 = 9 | | | | | | |
| 4 x 2 = 8 | 4 x 3 = 12 | 4 × 4 = 16 | | | | | |
| 5 x 2 = 10 | 5 x 3 = 15 | 5 x 4 = 20 | 5 x 5 = 25 | | | | |
| 6 x 2 = 12 | 6 x 3 = 18 | 6 x 4 = 24 | 6 x 5 = 30 | 6 x 6 = 36 | | | |
| 7 x 2 = 14 | 7 x 3 = 21 | 7 x 4 = 28 | 7 x 5 = 35 | 7 x 6 = 42 | 7 x 7 = 49 | | |
| 8 x 2 = 16 | 8 x 3 = 24 | 8 x 4 = 32 | 8 x 5 = 40 | 8 x 6 = 48 | 8 x 7 = 56 | 8 x 8 = 64 | |
| 9 x 2 = 18 | 9 x 3 = 27 | 9 x 4 = 36 | 9 x 5 = 45 | 9 x 6 = 54 | 9 x 7 = 63 | 9 x 8 = 72 | 9 x 9 = 81 |

Calculation Policy

To ensure there is progression built within the Maths curriculum, St. Mary's has adopted the White Rose Calculation policy. Below you will see models and images to support each concept for the four operations. There is also a glossary to support the key language used within school.

Examples of the models and tools used in school are followed by the key concepts taught in each year group.





Year 1 - 6

Calculation Policy Addition and Subtraction

#MathsEveryoneCan





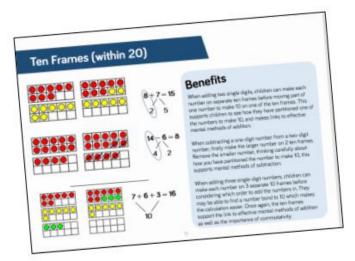
Notes and Guidance

Calculation Policy

Welcome to the White Rose Maths Calculation Policy.

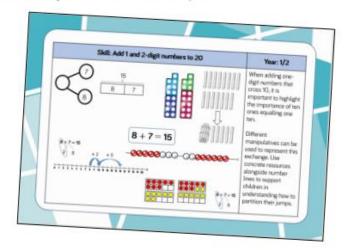
This document is broken down into addition and subtraction, and multiplication and division.

At the start of each policy, there is an overview of the different models and images that can support the teaching of different concepts. These provide explanations of the benefits of using the models and show the links between different operations.





Each operation is then broken down into skills and each skill has a dedicated page showing the different models and images that could be used to effectively teach that concept.

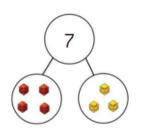


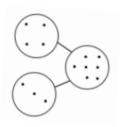
There is an overview of skills linked to year groups to support consistency through out school. A glossary of terms is provided at the end of the calculation policy to support understanding of the key language used to teach the four operations.

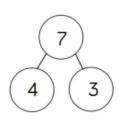




Part-Whole Model





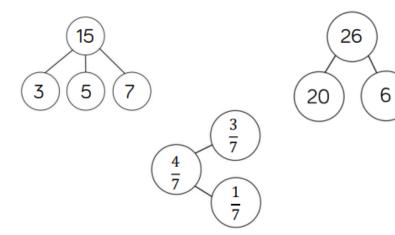


$$7 = 4 + 3$$

$$7 = 3 + 4$$

$$7 - 3 = 4$$

$$7 - 4 = 3$$



Benefits

This part-whole model supports children in their understanding of aggregation and partitioning. Due to its shape, it can be referred to as a cherry part-whole model.

When the parts are complete and the whole is empty, children use aggregation to add the parts together to find the total.

When the whole is complete and at least one of the parts is empty, children use partitioning (a form of subtraction) to find the missing part.

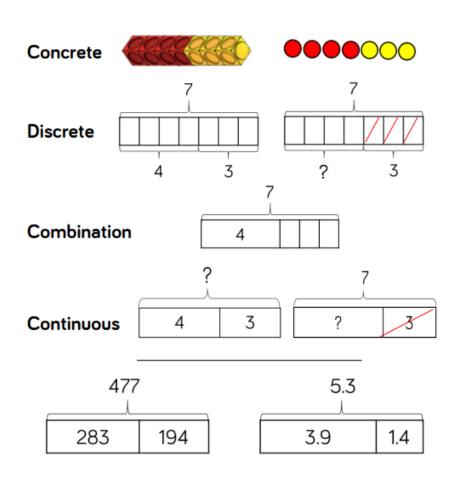
Part-whole models can be used to partition a number into two or more parts, or to help children to partition a number into tens and ones or other place value columns.

In KS2, children can apply their understanding of the part-whole model to add and subtract fractions, decimals and percentages.





Bar Model (single)



Benefits

The single bar model is another type of a part-whole model that can support children in representing calculations to help them unpick the structure.

Cubes and counters can be used in a line as a concrete representation of the bar model.

Discrete bar models are a good starting point with smaller numbers. Each box represents one whole.

The combination bar model can support children to calculate by counting on from the larger number. It is a good stepping stone towards the continuous bar model.

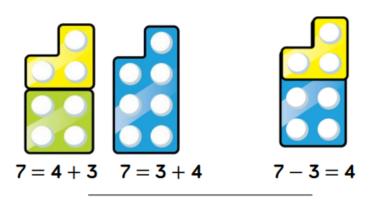
Continuous bar models are useful for a range of values. Each rectangle represents a number. The question mark indicates the value to be found.

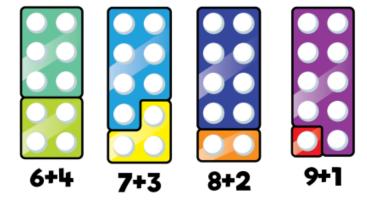
In KS2, children can use bar models to represent larger numbers, decimals and fractions.





Number Shapes





Benefits

Number shapes can be useful to support children to subitise numbers as well as explore aggregation, partitioning and number bonds.

When adding numbers, children can see how the parts come together making a whole. As children use number shapes more often, they can start to subitise the total due to their familiarity with the shape of each number.

When subtracting numbers, children can start with the whole and then place one of the parts on top of the whole to see what part is missing. Again, children will start to be able to subitise the part that is missing due to their familiarity with the shapes.

Children can also work systematically to find number bonds. As they increase one number by 1, they can see that the other number decreases by 1 to find all the possible number bonds for a number.





Cubes



$$7 = 4 + 3$$



$$7 = 3 + 4$$



$$7 - 3 = 4$$





$$7 - 3 = 4$$

Benefits

Cubes can be useful to support children with the addition and subtraction of one-digit numbers.

When adding numbers, children can see how the parts come together to make a whole. Children could use two different colours of cubes to represent the numbers before putting them together to create the whole.

When subtracting numbers, children can start with the whole and then remove the number of cubes that they are subtracting in order to find the answer. This model of subtraction is reduction, or take away.

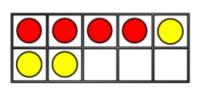
Cubes can also be useful to look at subtraction as difference. Here, both numbers are made and then lined up to find the difference between the numbers.

Cubes are useful when working with smaller numbers but are less efficient with larger numbers as they are difficult to subitise and children may miscount them.

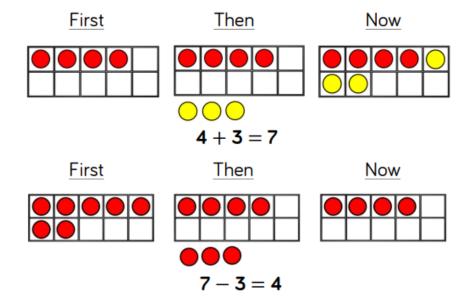




Ten Frames (within 10)



$$4+3=7$$
 4 is a part.
 $3+4=7$ 3 is a part.
 $7-3=4$ 7 is the whole.



Benefits

When adding and subtracting within 10, the ten frame can support children to understand the different structures of addition and subtraction.

Using the language of parts and wholes represented by objects on the ten frame introduces children to aggregation and partitioning.

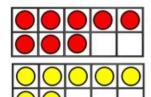
Aggregation is a form of addition where parts are combined together to make a whole. Partitioning is a form of subtraction where the whole is split into parts. Using these structures, the ten frame can enable children to find all the number bonds for a number.

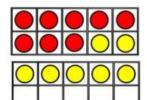
Children can also use ten frames to look at augmentation (increasing a number) and take-away (decreasing a number). This can be introduced through a first, then, now structure which shows the change in the number in the 'then' stage. This can be put into a story structure to help children understand the change e.g. First, there were 7 cars. Then, 3 cars left. Now, there are 4 cars.

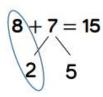


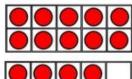


Ten Frames (within 20)

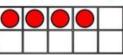




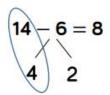


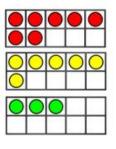


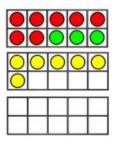


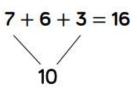












Benefits

When adding two single digits, children can make each number on separate ten frames before moving part of one number to make 10 on one of the ten frames. This supports children to see how they have partitioned one of the numbers to make 10, and makes links to effective mental methods of addition.

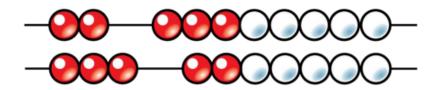
When subtracting a one-digit number from a two-digit number, firstly make the larger number on 2 ten frames. Remove the smaller number, thinking carefully about how you have partitioned the number to make 10, this supports mental methods of subtraction.

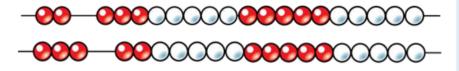
When adding three single-digit numbers, children can make each number on 3 separate 10 frames before considering which order to add the numbers in. They may be able to find a number bond to 10 which makes the calculation easier. Once again, the ten frames support the link to effective mental methods of addition as well as the importance of commutativity.





Bead Strings







Benefits

Different sizes of bead strings can support children at different stages of addition and subtraction.

Bead strings to 10 are very effective at helping children to investigate number bonds up to 10.

They can help children to systematically find all the number bonds to 10 by moving one bead at a time to see the different numbers they have partitioned the 10 beads into e.g. 2 + 8 = 10, move one bead, 3 + 7 = 10.

Bead strings to 20 work in a similar way but they also group the beads in fives. Children can apply their knowledge of number bonds to 10 and see the links to number bonds to 20.

Bead strings to 100 are grouped in tens and can support children in number bonds to 100 as well as helping when adding by making ten. Bead strings can show a link to adding to the next 10 on number lines which supports a mental method of addition.



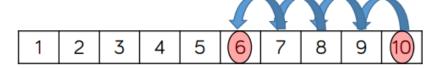


Number Tracks

$$5 + 3 = 8$$



$$10 - 4 = 6$$



$$8 + 7 = 15$$



Benefits

Number tracks are useful to support children in their understanding of augmentation and reduction.

When adding, children count on to find the total of the numbers. On a number track, children can place a counter on the starting number and then count on to find the total.

When subtracting, children count back to find their answer. They start at the minuend and then take away the subtrahend to find the difference between the numbers.

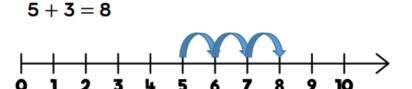
Number tracks can work well alongside ten frames and bead strings which can also model counting on or counting back.

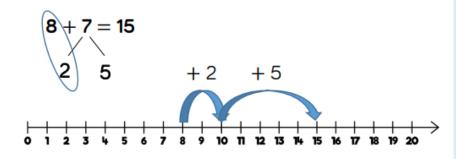
Playing board games can help children to become familiar with the idea of counting on using a number track before they move on to number lines.

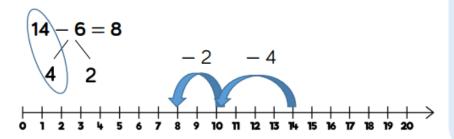




Number Lines (labelled)







Benefits

Labelled number lines support children in their understanding of addition and subtraction as augmentation and reduction.

Children can start by counting on or back in ones, up or down the number line. This skill links directly to the use of the number track.

Progressing further, children can add numbers by jumping to the nearest 10 and then jumping to the total. This links to the making 10 method which can also be supported by ten frames. The smaller number is partitioned to support children to make a number bond to 10 and to then add on the remaining part.

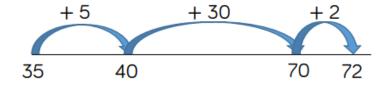
Children can subtract numbers by firstly jumping to the nearest 10. Again, this can be supported by ten frames so children can see how they partition the smaller number into the two separate jumps.



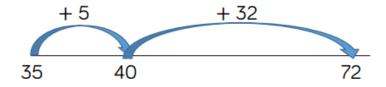


Number Lines (blank)

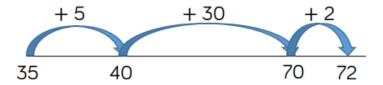
$$35 + 37 = 72$$



$$35 + 37 = 72$$



$$72 - 35 = 37$$



Benefits

Blank number lines provide children with a structure to add and subtract numbers in smaller parts.

Developing from labelled number lines, children can add by jumping to the nearest 10 and then adding the rest of the number either as a whole or by adding the tens and ones separately.

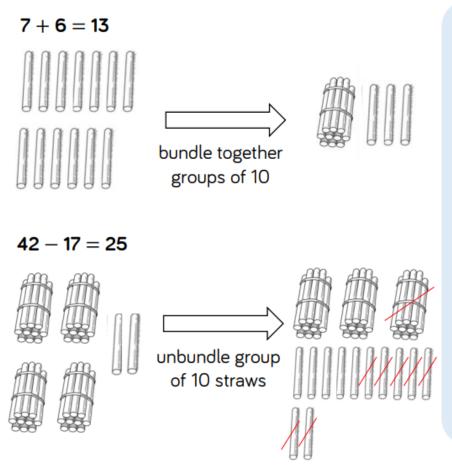
Children may also count back on a number line to subtract, again by jumping to the nearest 10 and then subtracting the rest of the number.

Blank number lines can also be used effectively to help children subtract by finding the difference between numbers. This can be done by starting with the smaller number and then counting on to the larger number. They then add up the parts they have counted on to find the difference between the numbers.





Straws



Benefits

Straws are an effective way to support children in their understanding of exchange when adding and subtracting 2-digit numbers.

Children can be introduced to the idea of bundling groups of ten when adding smaller numbers and when representing 2-digit numbers. Use elastic bands or other ties to make bundles of ten straws.

When adding numbers, children bundle a group of 10 straws to represent the exchange from 10 ones to 1 ten. They then add the individual straws (ones) and bundles of straws (tens) to find the total.

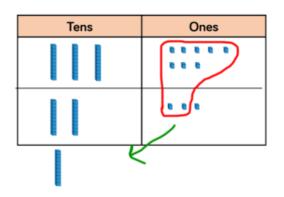
When subtracting numbers, children unbundle a group of 10 straws to represent the exchange from 1 ten to 10 ones.

Straws provide a good stepping stone to adding and subtracting with Base 10/Dienes.





Base 10/Dienes (addition)



$$\begin{array}{r}
 38 \\
 + 23 \\
 \hline
 61 \\
 \hline
 _{1}
 \end{array}$$

Hundreds	Tens	Ones	
			265
			+ 164
			429
			1
K			

Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.

Children should first add without an exchange before moving on to addition with exchange.. The representation becomes less efficient with larger numbers due to the size of Base 10. In this case, place value counters may be the better model to use.

When adding, always start with the smallest place value column. Here are some questions to support children. How many ones are there altogether?

Can we make an exchange? (Yes or No)

How many do we exchange? (10 ones for 1 ten, show exchanged 10 in tens column by writing 1 in column)

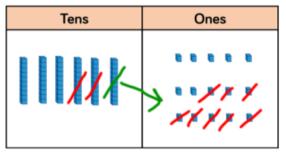
How many ones do we have left? (Write in ones column)

Repeat for each column.





Base 10/Dienes (subtraction)



Hundreds	Tens	Ones	3/125
		.411	-273
	J		162
	MM		

Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing Base 10 so they can see the clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. When building the model, children should just make the minuend using Base 10, they then subtract the subtrahend. Highlight this difference to addition to avoid errors by making both numbers. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.

This model is efficient with up to 4-digit numbers. Place value counters are more efficient with larger numbers and decimals.





Place Value Counters (addition)

Hundreds	Tens	Ones	
100 100 100	0000	0000	384
	10 10 10 10		+ 237
100 000	000	0000	621
	/		1 1
	0		,

Ones	Tenths	Hundredths	
000	01 01 01	(a) (a) (a)	3.65
	01 01 01	0.01 0.01	+ 2.41
00	01 01 01	001	6.06
	(01)		1

Benefits

Using place value counters is an effective way to support children's understanding of column addition. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

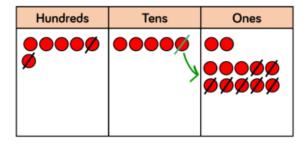
Children should first add without an exchange before moving on to addition with exchange. Different place value counters can be used to represent larger numbers or decimals. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When adding money, children can also use coins to support their understanding. It is important that children consider how the coins link to the written calculation especially when adding decimal amounts.





Place Value Counters (Subtraction)



$$\begin{array}{r}
652 \\
-207 \\
445
\end{array}$$

Thousands	Hundreds	Tens	Ones	_ 1
	100 100			³ 4357
	00000			– 2735
/	& & & & & & & & & &			1622

Benefits

Using place value counters is an effective way to support children's understanding of column subtraction. It is important that children write out their calculations alongside using or drawing counters so they can see the clear links between the written method and the model.

Children should first subtract without an exchange before moving on to subtraction with exchange. If you don't have place value counters, use normal counters on a place value grid to enable children to experience the exchange between columns.

When building the model, children should just make the minuend using counters, they then subtract the subtrahend. Children start with the smallest place value column. When there are not enough ones/tens/hundreds to subtract in a column, children need to move to the column to the left and exchange e.g. exchange 1 ten for 10 ones. They can then subtract efficiently.

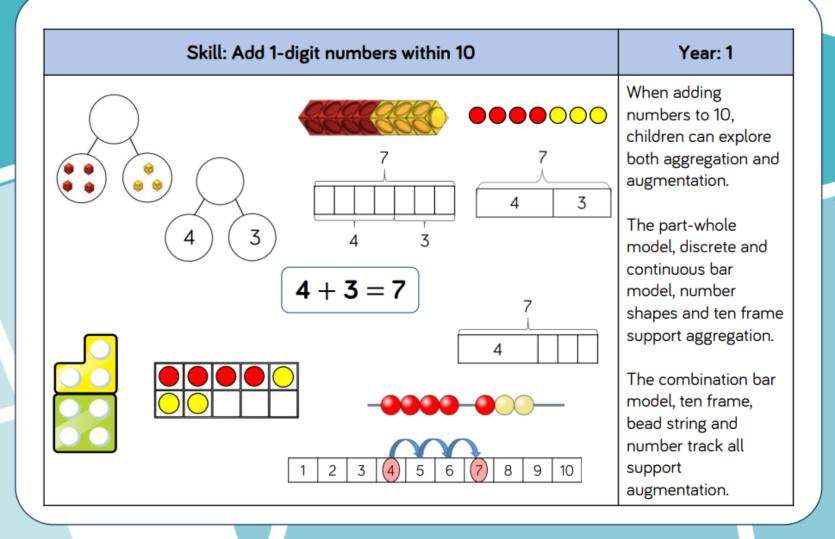




Addition

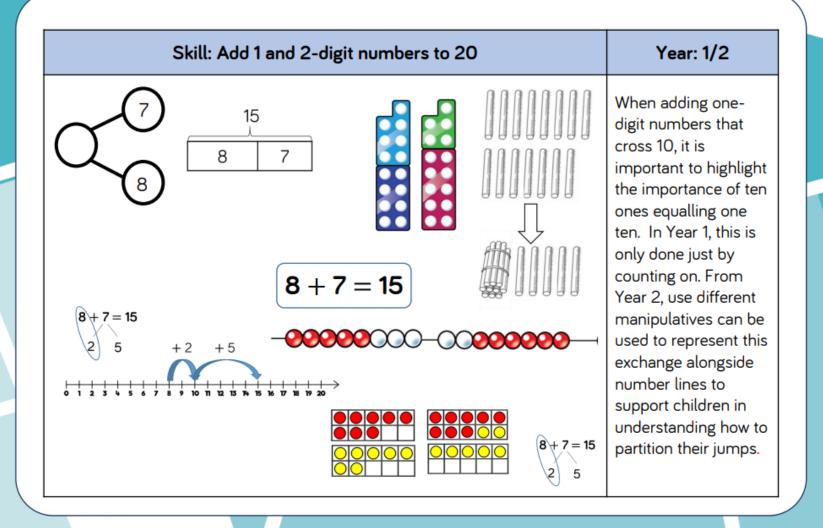






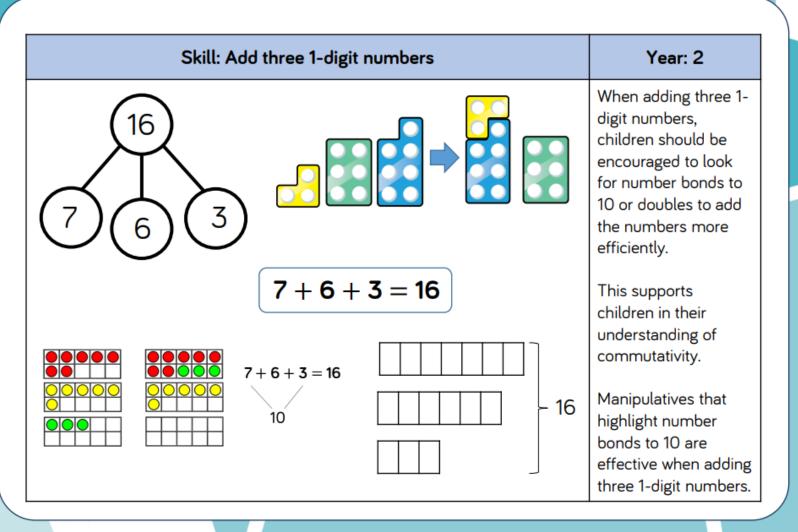






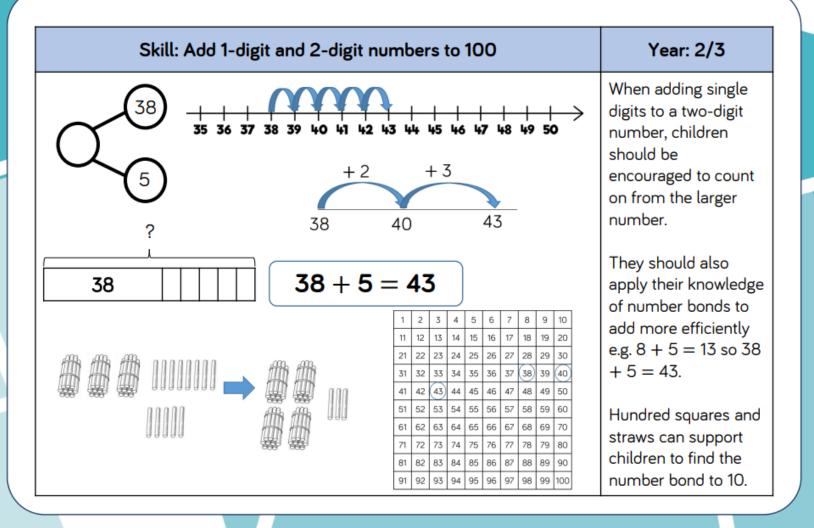






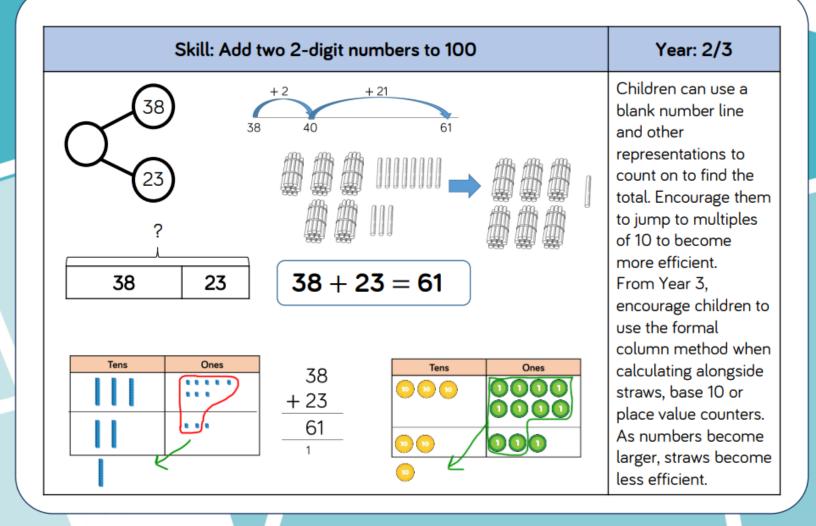






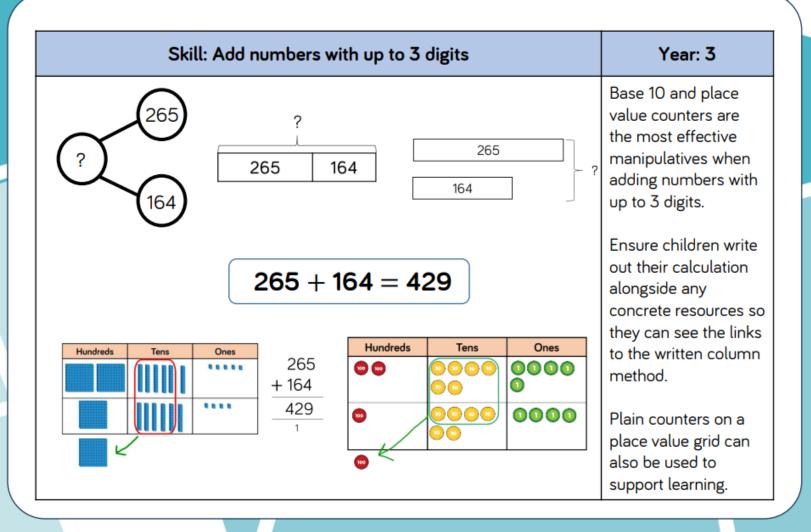








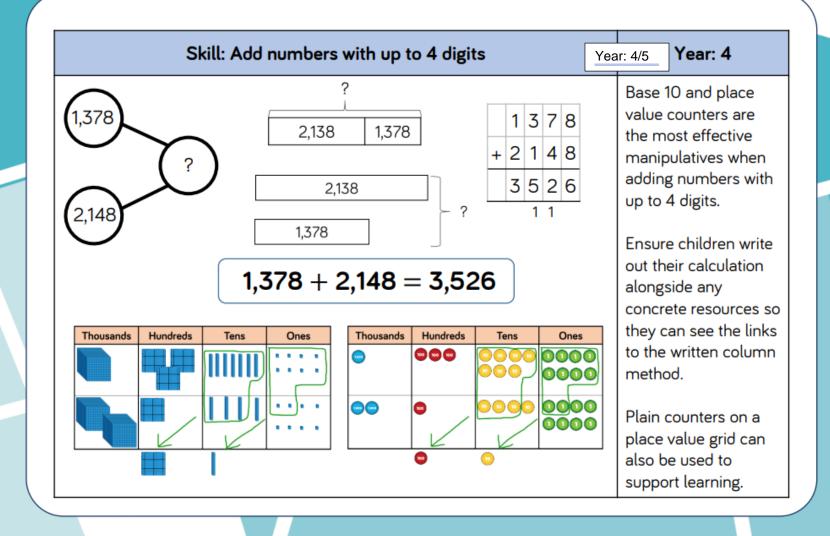






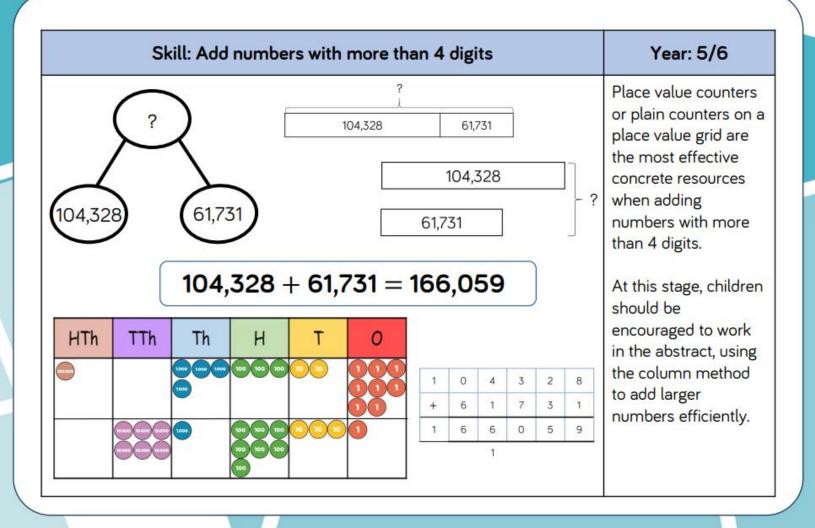






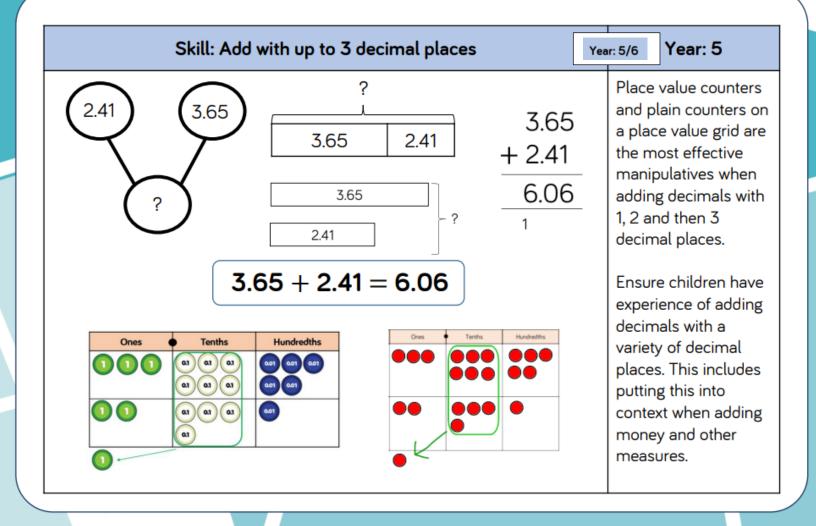












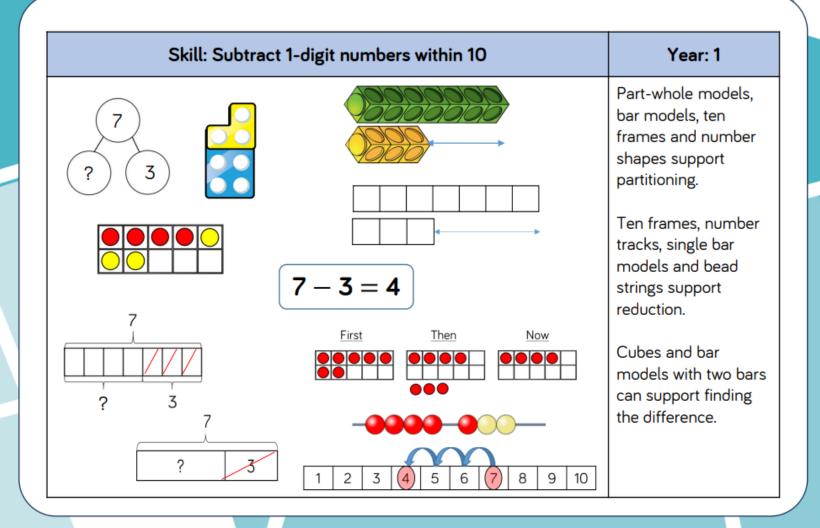




Subtraction

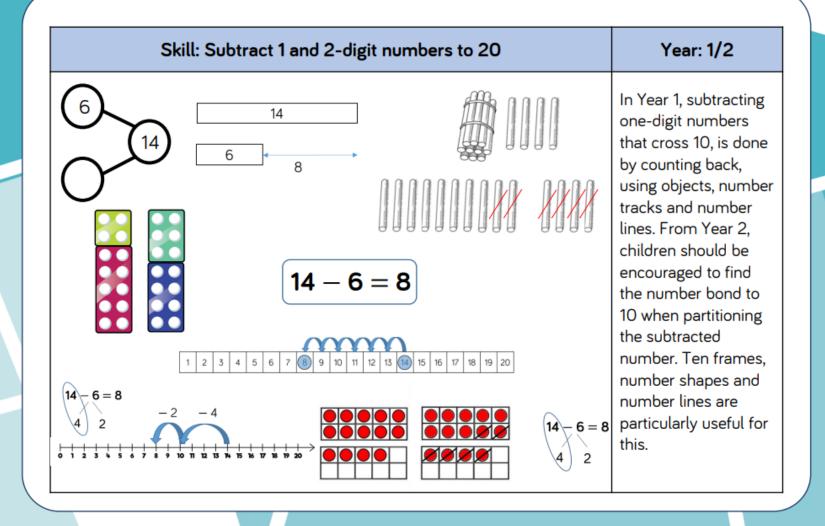






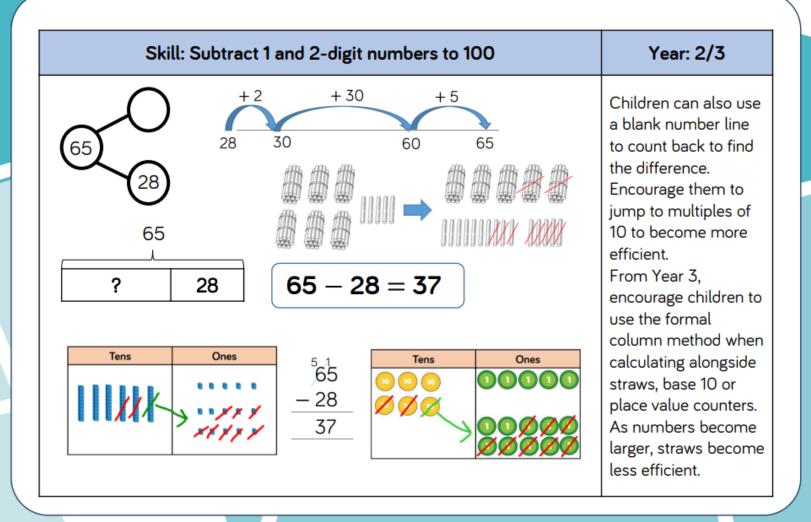






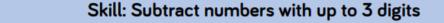


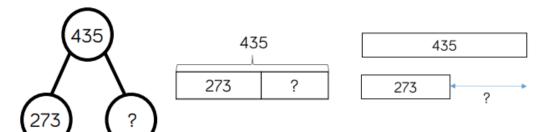












$$435 - 273 = 162$$

Hundreds	Tens	Ones	3/125
		.111	– 273
	J		162
	" MM		

Hundreds	Tens	Ones
0000	000	OOØØ
V	000ØØ ØØØØØ	

Base 10 and place value counters are the most effective manipulative when

Year: 3

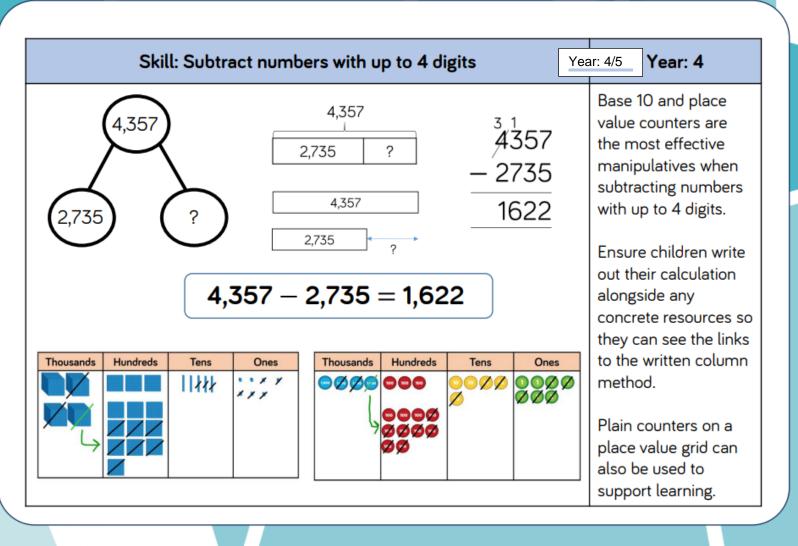
subtracting numbers with up to 3 digits.

Ensure children write out their calculation alongside any concrete resources so they can see the links to the written column method.

Plain counters on a place value grid can also be used to support learning.

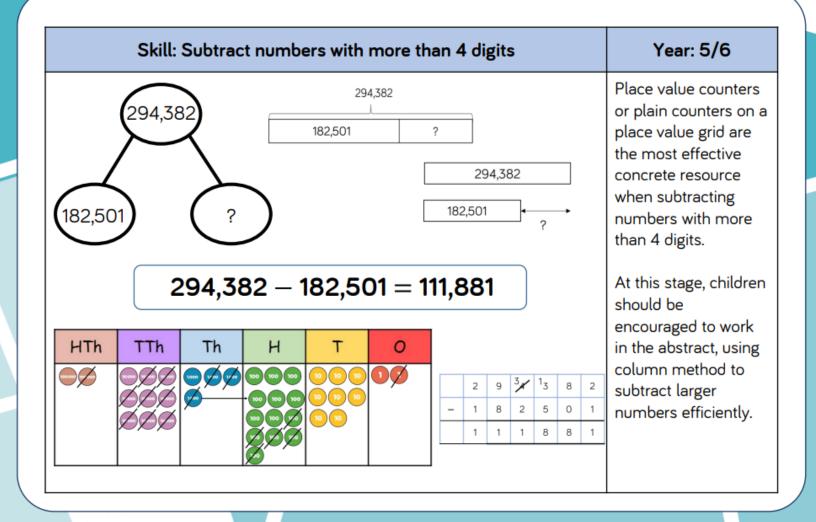






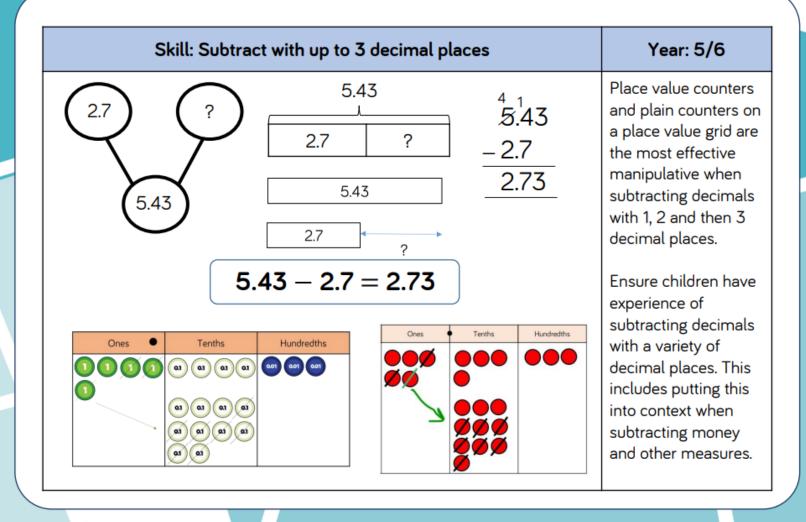
















Glossary

Addend - A number to be added to another.

Aggregation - combining two or more quantities or measures to find a total.

Augmentation - increasing a quantity or measure by another quantity.

Commutative - numbers can be added in any order.

Complement – in addition, a number and its complement make a total e.g. 300 is the complement to 700 to make 1,000

Difference – the numerical difference between two numbers is found by comparing the quantity in each group.

Exchange – Change a number or expression for another of an equal value.

Minuend – A quantity or number from which another is subtracted.

Partitioning – Splitting a number into its component parts.

Reduction - Subtraction as take away.

Subitise – Instantly recognise the number of objects in a small group without needing to count.

Subtrahend - A number to be subtracted from another.

Sum - The result of an addition.

Total - The aggregate or the sum found by addition.





Year 1 - 6

Calculation Policy Multiplication and Division

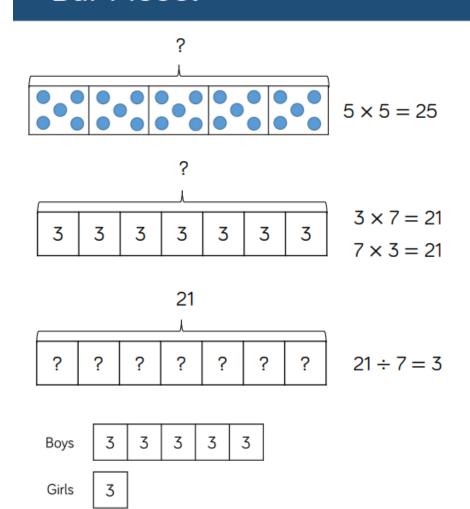
#MathsEveryoneCan

White Rose Maths





Bar Model



Benefits

Children can use the single bar model to represent multiplication as repeated addition. They could use counters, cubes or dots within the bar model to support calculation before moving on to placing digits into the bar model to represent the multiplication.

Division can be represented by showing the total of the bar model and then dividing the bar model into equal groups.

It is important when solving word problems that the bar model represents the problem.

Sometimes, children may look at scaling problems. In this case, more than one bar model is useful to represent this type of problem, e.g. There are 3 girls in a group. There are 5 times more boys than girls. How many boys are there?

The multiple bar model provides an opportunity to compare the groups.



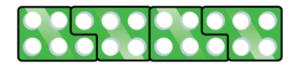


Number Shapes



 $5 \times 4 = 20$

 $4 \times 5 = 20$

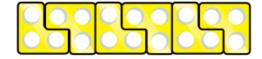


 $5 \times 4 = 20$

 $4 \times 5 = 20$



 $18 \div 3 = 6$



Benefits

Number shapes support children's understanding of multiplication as repeated addition.

Children can build multiplications in a row using the number shapes. When using odd numbers, encourage children to interlock the shapes so there are no gaps in the row. They can then use the tens number shapes along with other necessary shapes over the top of the row to check the total. Using the number shapes in multiplication can support children in discovering patterns of multiplication e.g. odd \times odd = even, odd \times even = odd, even \times even = even.

When dividing, number shapes support children's understanding of division as grouping. Children make the number they are dividing and then place the number shape they are dividing by over the top of the number to find how many groups of the number there are altogether e.g. There are 6 groups of 3 in 18.





Bead Strings



$$5 \times 3 = 15$$

 $3 \times 5 = 15$

$$15 \div 3 = 5$$



$$5 \times 3 = 15$$

 $3 \times 5 = 15$

$$15 \div 5 = 3$$



$$4 \times 5 = 20$$

$$5 \times 4 = 20$$

$$20 \div 4 = 5$$

Benefits

Bead strings to 100 can support children in their understanding of multiplication as repeated addition. Children can build the multiplication using the beads. The colour of beads supports children in seeing how many groups of 10 they have, to calculate the total more efficiently.

Encourage children to count in multiples as they build the number e.g. 4, 8, 12, 16, 20.

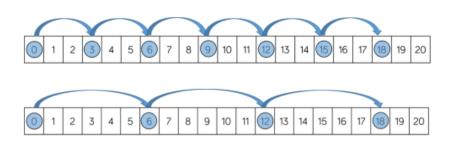
Children can also use the bead string to count forwards and backwards in multiples, moving the beads as they count.

When dividing, children build the number they are dividing and then group the beads into the number they are dividing by e.g. 20 divided by 4 – Make 20 and then group the beads into groups of four. Count how many groups you have made to find the answer.



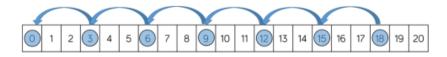


Number Tracks



$$6 \times 3 = 18$$

 $3 \times 6 = 18$



 $18 \div 3 = 6$

Benefits

Number tracks are useful to support children to count in multiples, forwards and backwards. Moving counters or cubes along the number track can support children to keep track of their counting. Translucent counters help children to see the number they have landed on whilst counting.

When multiplying, children place their counter on 0 to start and then count on to find the product of the numbers.

When dividing, children place their counter on the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0. Children record how many jumps they have made to find the answer to the division.

Number tracks can be useful with smaller multiples but when reaching larger numbers they can become less efficient.





Number Lines (labelled)





$$4 \times 5 = 20$$

 $5 \times 4 = 20$



 $20 \div 4 = 5$

Benefits

Labelled number lines are useful to support children to count in multiples, forwards and backwards as well as calculating single-digit multiplications.

When multiplying, children start at 0 and then count on to find the product of the numbers.

When dividing, start at the number they are dividing and the count back in jumps of the number they are dividing by until they reach 0.

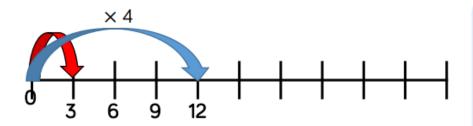
Children record how many jumps they have made to find the answer to the division.

Labelled number lines can be useful with smaller multiples, however they become inefficient as numbers become larger due to the required size of the number line.

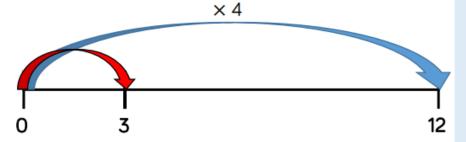




Number Lines (blank)



A red car travels 3 miles. A blue car 4 times further. How far does the blue car travel?



A blue car travels 12 miles. A red car 4 times less. How far does the red car travel?

Benefits

Children can use blank number lines to represent scaling as multiplication or division.

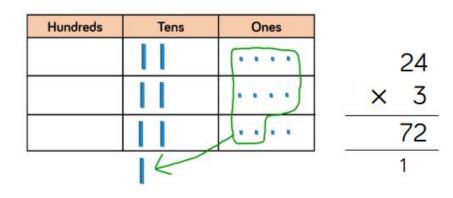
Blank number lines with intervals can support children to represent scaling accurately. Children can label intervals with multiples to calculate scaling problems.

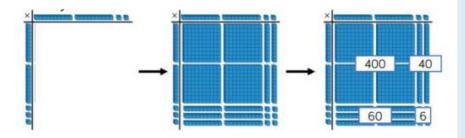
Blank number lines without intervals can also be used for children to represent scaling.





Base 10/Dienes (multiplication)





Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written representations match.

As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed.

Base 10 also supports the area model of multiplication well. Children use the equipment to build the number in a rectangular shape which they then find the area of by calculating the total value of the pieces This area model can be linked to the grid method or the formal column method of multiplying 2-digits by 2-digits.



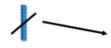


Base 10/Dienes (division)



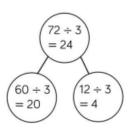


$$68 \div 2 = 34$$



Tens	Ones
	•
	•
	• • • •

$$72 \div 3 = 24$$



Benefits

Using Base 10 or Dienes is an effective way to support children's understanding of division.

When numbers become larger, it can be an effective way to move children from representing numbers as ones towards representing them as tens and ones in order to divide. Children can then share the Base 10/ Dienes between different groups e.g. by drawing circles or by rows on a place value grid.

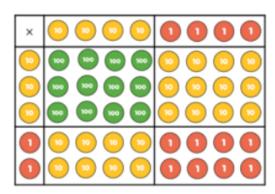
When they are sharing, children start with the larger place value and work from left to right. If there are any left in a column, they exchange e.g. one ten for ten ones. When recording, encourage children to use the partwhole model so they can consider how the number has been partitioned in order to divide. This will support them with mental methods.





Place Value Counters (multiplication)

Hundreds	Tens	Ones
	000	0000
	000	0000
	000	0000
	000	0000
	000	0000
	20	



		44
	×	32
		8
		80
	•	120
+	12	200
	14	804
	1	

Benefits

Using place value counters is an effective way to support children's understanding of column multiplication. It is important that children write out their calculation alongside the equipment so they can see how the concrete and written match.

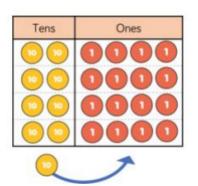
As numbers become larger in multiplication or the amounts of groups becomes higher, Base 10 / Dienes becomes less efficient due to the amount of equipment and number of exchanges needed The counters should be used to support the understanding of the written method rather than support the arithmetic.

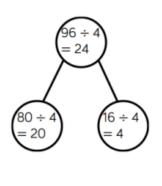
Place value counters also support the area model of multiplication well. Children can see how to multiply 2-digit numbers by 2-digit numbers.

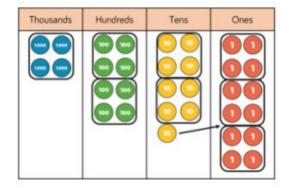




Place Value Counters (division)







1223 4 489¹2

Benefits

Using place value counters is an effective way to support children's understanding of division.

When working with smaller numbers, children can use place value counters to share between groups. They start by sharing the larger place value column and work from left to right. If there are any counters left over once they have been shared, they exchange the counter e.g. exchange one ten for ten ones. This method can be linked to the part-whole model to support children to show their thinking.

Place value counters also support children's understanding of short division by grouping the counters rather than sharing them. Children work from left to right through the place value columns and group the counters in the number they are dividing by. If there are any counters left over after they have been grouped, they exchange the counter e.g. exchange one hundred for ten tens.





Times Tables

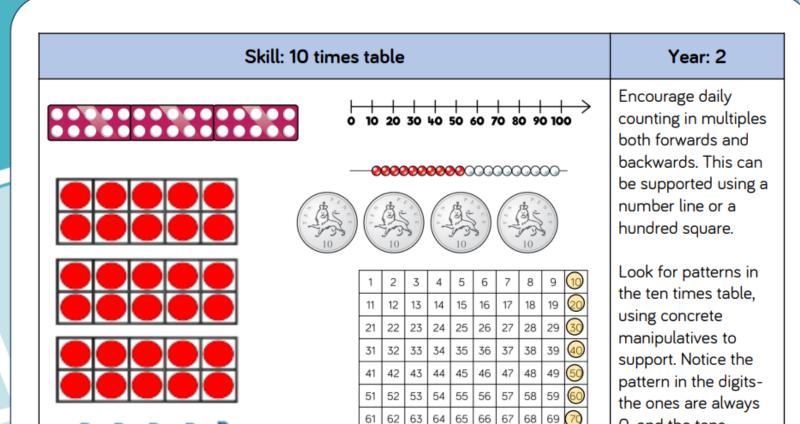




0, and the tens

each time.

increase by 1 ten



73 74 75 76 77

92 93 94 95 96 97

83

84 85 86 87

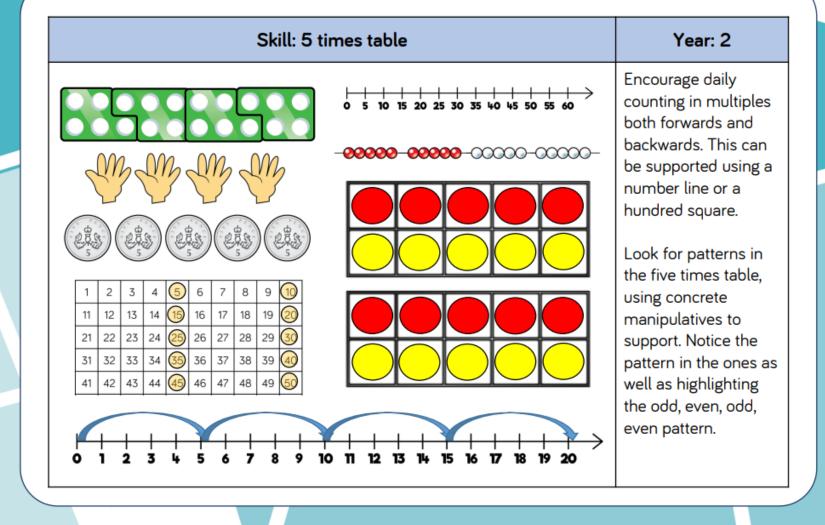
78 79

88 89

98 99

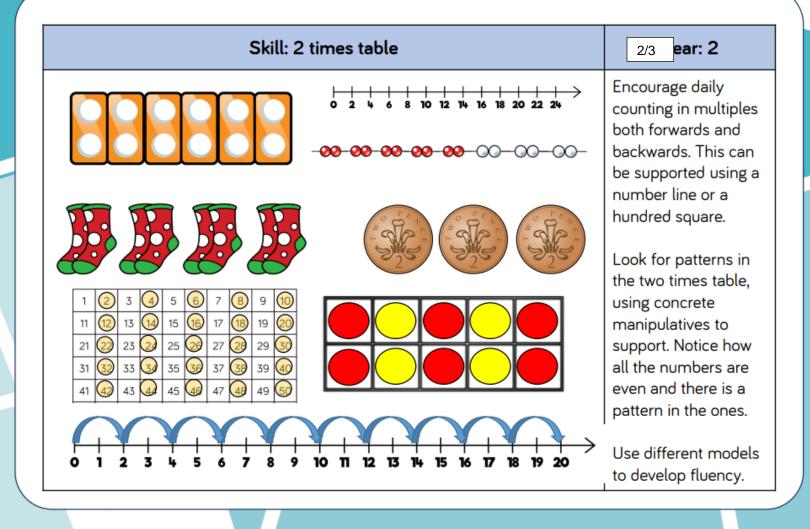






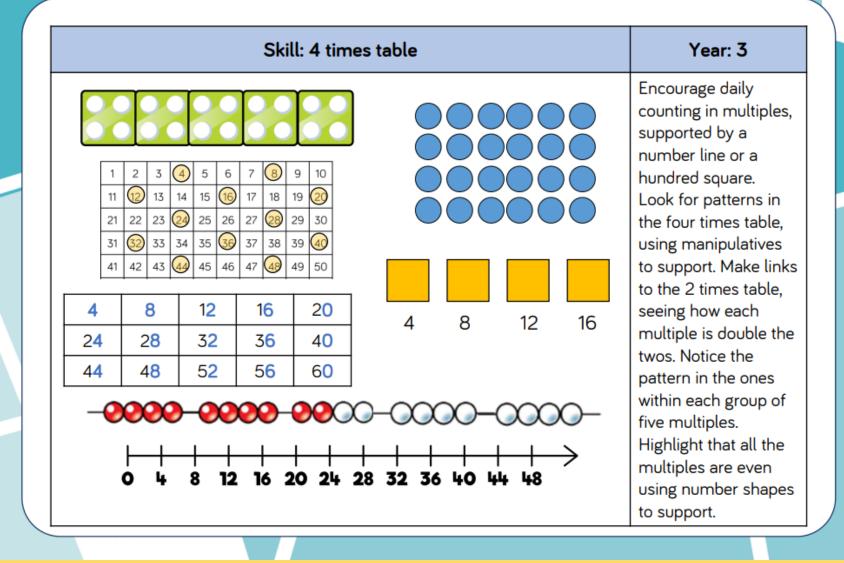






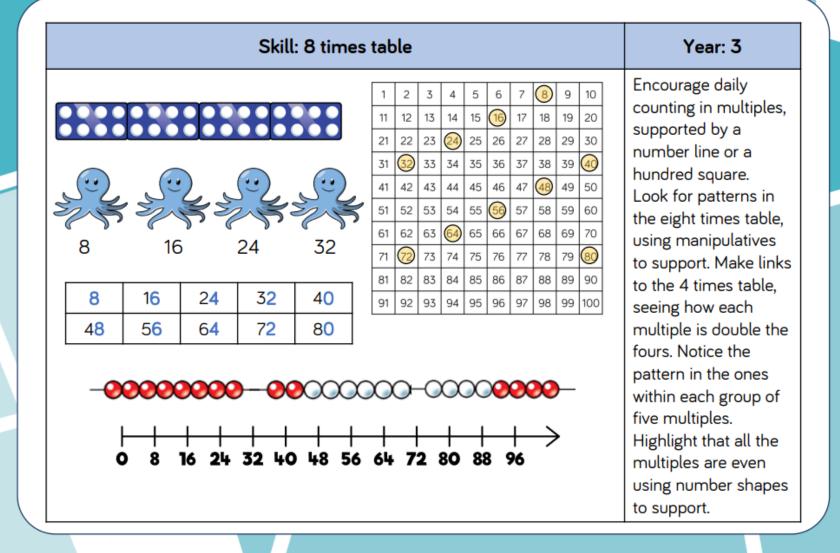








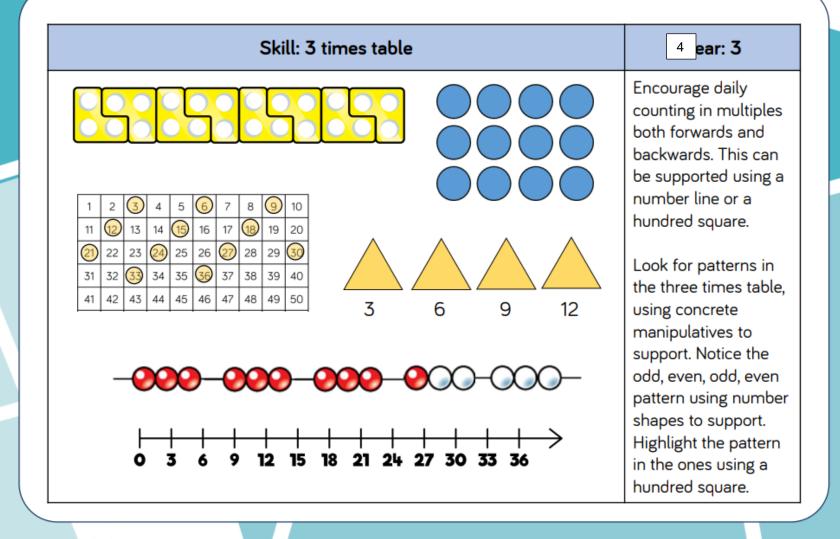






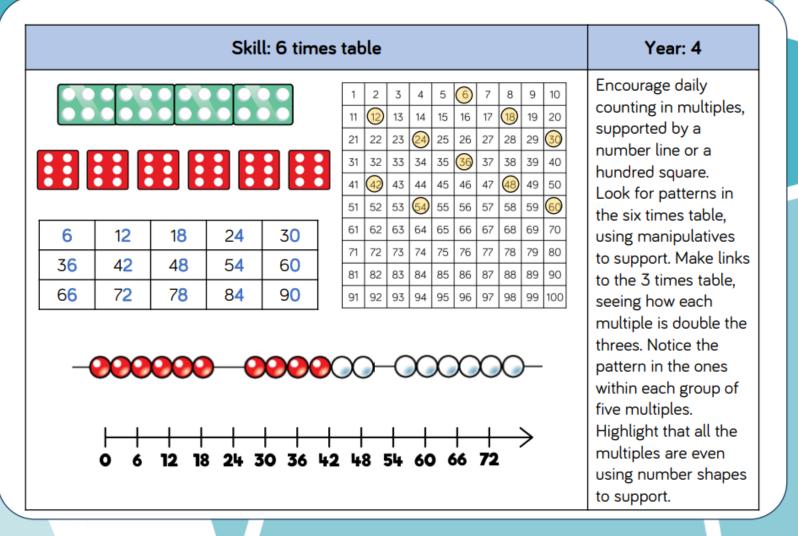














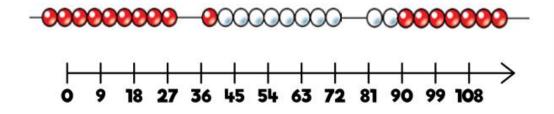






9	18	27	36	45
54	63	72	81	90

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	64)	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	9
91	92	93	94	95	96	97	98	9	100



Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the nine times table. using concrete manipulatives to support. Notice the pattern in the tens and ones using the hundred square to support as well as noting the odd, even pattern within the multiples.

Year: 4



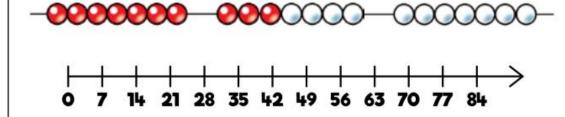






 7	14	21	28	35
42	49	56	63	70

1	2	3	4	5	6	7	8	9	10
11	12	13	14)	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35)	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	66	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	7	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	9	99	100



Year: 4

Encourage daily counting in multiples both forwards and backwards, supported by a number line or a hundred square. The seven times table can be trickier to learn due to the lack of obvious pattern in the numbers, however they already know several facts due to commutativity. Children can still see the odd, even pattern in the multiples using number shapes to support.

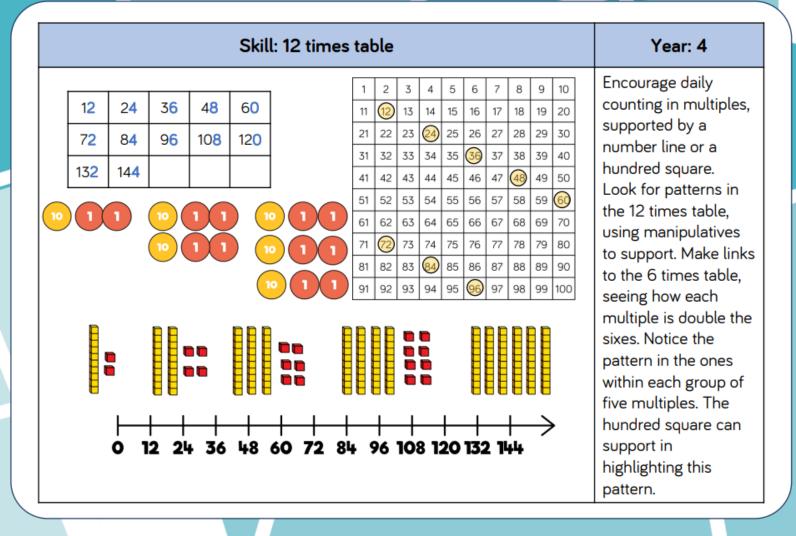




Skill: 11 times table														Year: 4			
11 77	22 88	33 99	110	55 121	66 132		1 11 21 31 41 51 61 71 81	2 12 32 42 52 62 72 82 92	3 13 23 43 53 63 73 83 93	4 14 24 34 54 64 74 84 94	5 15 25 35 45 65 75 85 95	66	7 17 27 37 47 57 67 7 87	8 18 28 38 48 58 68 78 83 98	79 89	10 20 30 40 50 60 70 80 90	Encourage daily counting in multiples both forwards and backwards. This can be supported using a number line or a hundred square. Look for patterns in the eleven times table, using concrete manipulatives to
	► O 1	1 22	33	+	+ 55 6	6 77	7 8	8	99	11	- O	12	1 13	 52			support. Notice the pattern in the tens and ones using the hundred square to support. Also consider the pattern after crossing 100











Multiplication





Skill:	Solve 1-step problems using multiplication	Year: 1/2
		Children represent multiplication as repeated addition in many different ways.
	0 1 2 3 4 5 6 7 8 9 10 11 12 13 74 15 16 17 18 19 20	In Year 1, children use concrete and pictorial
	One bag holds 5 apples. How many apples do 4 bags hold?	representations to solve problems. They are not expected to
		record multiplication formally.
	$5+5+5+5=20$ $4 \times 5 = 20$	In Year 2, children are introduced to the multiplication symbol.
	$5 \times 4 = 20$	





	Skil	l: Mu	ıltipl	y 2-c	digit num	bers by	/ 1-d	igit	nuı	mb	ers	Year: 3/4
Hundre	×		Tens T 3		34 × 5	5 = 17		1 1 1 O O O O O O O O O O O O O O O O O	T 3 2 5 7	0 4 5 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	(5 × 4) (5 × 30)	Informal methods and the expanded method are used in Year 3 before moving on to the short multiplication method in Year 4. Place value counters should be used to support the understanding of the method rather than supporting the multiplication, as children should use times table knowledge.





Ski	ll: Multiply	3-digit num	bers by 1-di	git r	numl	oers		Year: 4
Hundreds	Tens	Ones	4 = 980	×	H 2 9 1	T 4 8 2	0 5 4 0	When moving to 3-digit by 1-digit multiplication, encourage children to move towards the short, formal written method. Base 10 and place value counters continue to support the understanding of the written method. Limit the number of exchanges needed in
		W W W W W W W W W W	10 10 10 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0 (0	10 10 10 10 10 10 10 10 10 10 10 10 10 1	0(the questions and move children away from resources when multiplying larger numbers.



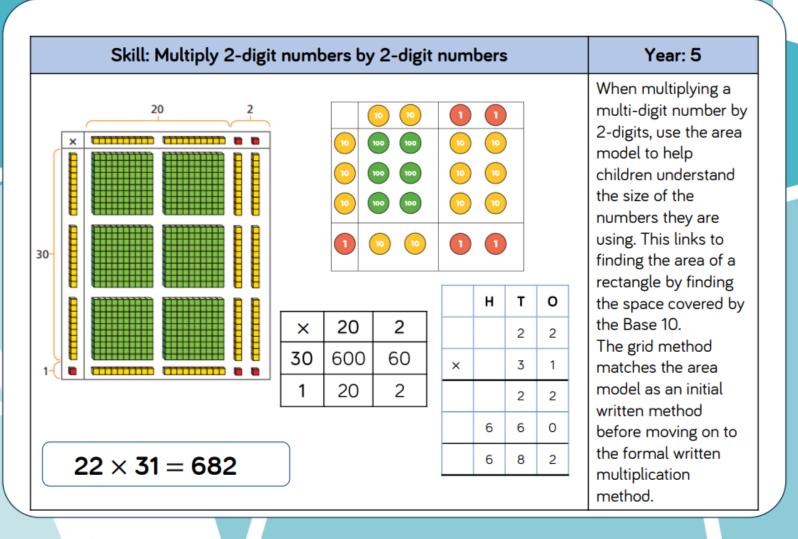




Skill: Multip	ly 4-digit	nur	mbe	rs by	y 1-c	ligit numbers	Year: 5
Thousands 1000 1000 1000	Hundred 100 100 100 100 100 100 100 100 100 100 100	0 100	000	10	,47		When multiplying 4-digit numbers, place value counters are the best manipulative to use to support children in their understanding of the formal written method. If children are multiplying larger
		Th	н	Т	0		numbers and struggling with their
		1	8	2	6		times tables,
	×				3		encourage the use of multiplication grids so
		5	4	7	8		children can focus or
		2		1			the use of the writter method.











Skill: Multiply 3-digit numbers by 2-digit numbers

100	100	10 10 10	0000
1000		100 100 100	10 10 10
1000			10 10 10 10
100		10 10 10	0000
100	100	10 10 10	000

Th	Н	Т	0
	2	3	4
×		3	2
	4	6	8
1 7	10	2	0
7	4	8	8

X	200	50	4
30	6,000	900	120
2	400	60	8

Children can continue to use the area model when multiplying 3-digits by 2-digits. Place value counters become more efficient to use but Base 10 can be used to highlight the size of numbers.

Year: 5

Children should now move towards the formal written method, seeing the links with the grid method.

234	×	32	=	7	48	8
237		J_			$\overline{}$	·





Skill: Multiply 4-digit numbers	by 2-digit numbers
---------------------------------	--------------------

TTh	Th	Н	Т	0
	2	7	3	9
×			2	8
2	1 5	9	1 7	2
5 1	4	7	8	0
7	6	6	9	2

When multiplying 4digits by 2-digits, children should be confident in using the formal written method.

Year: 5/6

If they are still struggling with times tables, provide multiplication grids to support when they are focusing on the use of the method.

Consider where exchanged digits are placed and make sure this is consistent.

 $2,739 \times 28 = 76,692$





Division

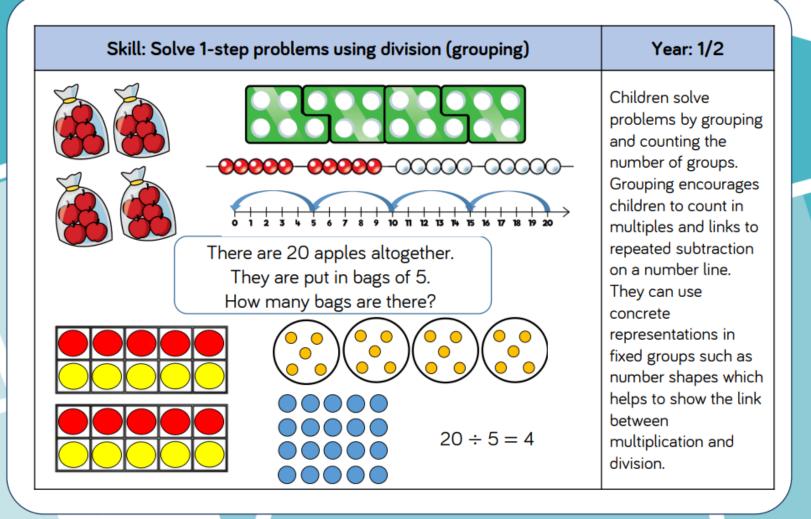




Skill: Solve 1-step problems using m	Year: 1/2	
	20 ? ? ? ? ?	Children solve problems by sharing amounts into equal groups.
There are 20 apples They are shared equally How many apples are	In Year 1, children use concrete and pictorial representations to solve problems. They are not expected to record division	
	20 ÷ 5 = 4	formally. In Year 2, children are introduced to the division symbol.

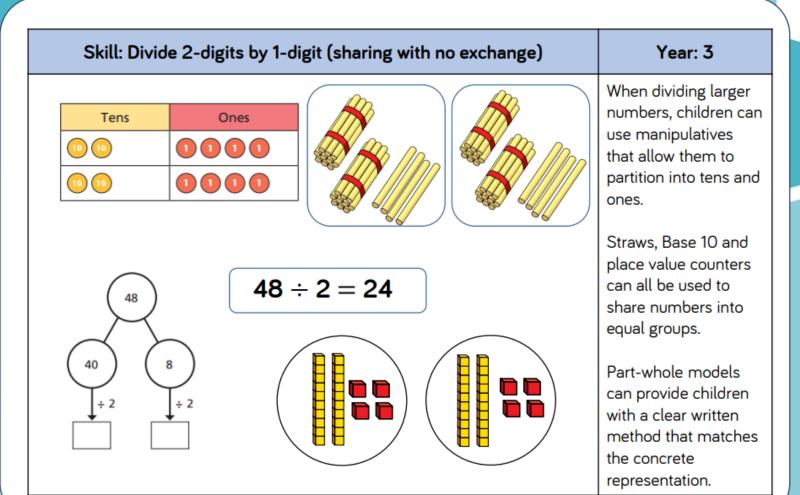
















Skill: Divide 2-digits by 1-d	ligit (sharing with exchange)	Year: 3/4
Tens Ones $ \begin{array}{cccccccccccccccccccccccccccccccccc$	52 ? ? ? ? ? 4 = 13 Tens Ones O 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	When dividing numbers involving an exchange, children can use Base 10 and place value counters to exchange one ten for ten ones. Children should start with the equipment outside the place value grid before sharing the tens and ones equally between the rows. Flexible partitioning in a part-whole model supports this method.





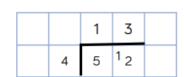
Skill: Divide	2-digits by 1-d	digit (sharing with remainders)	Year: 3/4
Tens 53 40 13 12 10 3	Ones 53 -	53 13 13 13 13 1	When dividing numbers with remainders, children can use Base 10 and place value counters to exchange one ten for ten ones. Starting with the equipment outside the place value grid will highlight remainders, as they will be left outside the grid once the equal groups have been made. Flexible partitioning in a part-whole model supports this method

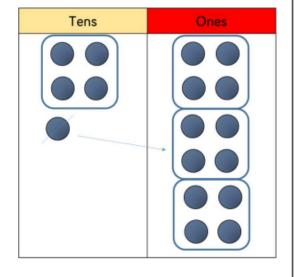




Skill: Divide 2-digits by 1-digit (grouping)

$$52 \div 4 = 13$$





When using the short division method, children use grouping. Starting with the largest place value, they group by the divisor.

Year: 5

Language is important here. Children should consider 'How many groups of 4 tens can we make?' and 'How many groups of 4 ones can we make?'

Remainders can also be seen as they are left ungrouped.





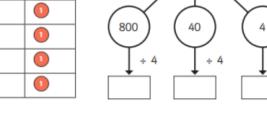
Skill: Divide	3-digits b	y 1-digit (sharing)
---------------	------------	-------------	----------

 $844 \div 4 = 211$

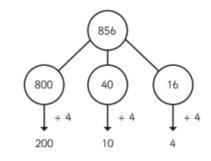
844 J					
?	?	?	?		

011

Н	Т	0
100 100	10	0
100 100	00	0
100 100	10	0
100 100	10	1



$$856 \div 4 = 214$$



		00000
Hundreds	Tens	Ones
100 100	10	0000
100 100	10	0000
100 100	10	0000
100 100	10	

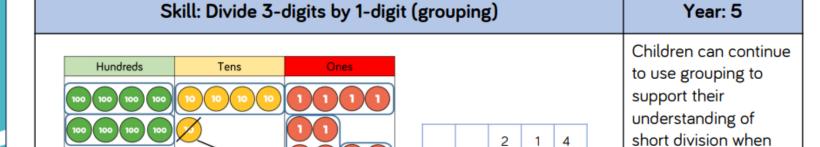
Year: 4

Children can continue to use place value counters to share 3-digit numbers into equal groups.
Children should start with the equipment outside the place value grid before sharing the hundreds, tens and ones equally between the rows.
This method can also help to highlight remainders.

Flexible partitioning in a part-whole model supports this method.







Hundreds Tens Ones

Place value counters or plain counters can be used on a place value grid to support this understanding. Children can also draw their own counters and group them through a more pictorial method.

dividing a 3-digit number by a 1-digit

number.

 $856 \div 4 = 214$





Th H T O

	4	2	6	6
2	8	5	13	12

Place value counters or plain counters can be used on a place value grid to support children to divide 4-digits by 1-digit. Children can also draw their own counters and group them through a more pictorial method.

Year: 5

Children should be encouraged to move away from the concrete and pictorial when dividing numbers with multiple exchanges.

$$8,532 \div 2 = 4,266$$





Skill: Divide multi digits by	2-digits (short division)
-------------------------------	---------------------------

0 3 6 12 4 4 3 7 2

$$432 \div 12 = 36$$

 $7,335 \div 15 = 489$

	0	4	8	9
15	7	⁷ ₃	13 3	13 ₅

15	30	45	60	75	90	105	120	135	150
----	----	----	----	----	----	-----	-----	-----	-----

When children begin to divide up to 4digits by 2-digits, written methods become the most accurate as concrete and pictorial representations become less effective. Children can write out multiples to support their calculations with larger remainders. Children will also solve problems with remainders where the quotient can be rounded as appropriate.

Year: 6





Skill: Divide multi-digits by 2-digits (long division						ion)	Year: 6	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			43	32	÷	12 =	= 36	Children can also divide by 2-digit numbers using long division. Children can write out multiples to support their calculations with larger remainders.
		0	4	8	9			
	15	7	3	3	5		$1 \times 15 = 15$	Children will also
	_	6	0	0	0	(×400	$2 \times 15 = 30$	solve problems with
$7,335 \div 15 = 489$		1	3	3	5		$3 \times 15 = 45$	remainders where the
7,555 - 15 - 469	_	1	2	0	0	(×80)	$4 \times 15 = 60$	quotient can be
			1	3	5		$5 \times 15 = 75$	rounded as
	-		1	3	5	(×9)	$10 \times 15 = 150$	appropriate.
					_		ì	





Ortice Project Organis Cy E Organis (toring Ortision)	Skill: Divide multi	i digits by 2-d	igits (long	division)
---	---------------------	-----------------	-------------	-----------

 $372 \div 15 = 24 \text{ r} 12$

			2	4	r	1	2
1	5	3	7	2			
	_	3	0	0			
			7	2			
	-		6	0			
			1	2			

$$1 \times 15 = 15$$

 $2 \times 15 = 30$
 $3 \times 15 = 45$
 $4 \times 15 = 60$
 $5 \times 15 = 75$
 $10 \times 15 = 150$

This will depend on the context of the question.

Children can also answer questions where the quotient needs to be rounded

according to the

context.

Year: 6

When a remainder is

left at the end of a

calculation, children

can either leave it as a

remainder or convert

it to a fraction.

			2	4	
1	5	3	7	2	
	_	3	0	0	
			7	2	
	_		6	0	
			1	2	

$$372 \div 15 = 24 \frac{4}{5}$$





Glossary

Array – An ordered collection of counters, cubes or other item in rows and columns.

Commutative – Numbers can be multiplied in any order.

Dividend – In division, the number that is divided.

Divisor – In division, the number by which another is divided.

Exchange – Change a number or expression for another of an equal value.

Factor – A number that multiplies with another to make a product.

Multiplicand – In multiplication, a number to be multiplied by another.

Partitioning – Splitting a number into its component parts.

Product – The result of multiplying one number by another.

Quotient - The result of a division

Remainder – The amount left over after a division when the divisor is not a factor of the dividend.

Scaling - Enlarging or reducing a number by a given amount, called the scale factor



